

Simplified Modelling Method of Impact Damage for Numerical Simulation of Lamb Wave Propagation in Quasi-isotropic Composite Structures

Research Background

The structural components suffer from **impact damage**, which is one of the **most fatal** damage for composites caused by a collision with objects or tool drops. Therefore, we are developing **health monitoring systems using ultrasonic Lamb waves** to detect impact damage in **CFRP structures**. In order to improve the system performance, **FEM simulation** is helpful because the wave propagation behavior in the structures can be clarified. However, an impact damage is **complex to be modeled precisely** because it consists of **multiple microscopic damages**. Hence, in this research, we attempt to establish a **simplified modeling method** of the impact damage.

Investigation of Impact Damage

CFRP **quasi-isotropic** laminates (T700S/2500, [45/0/-45/90]_{3s}) with 200mm in length and width and 3.4mm in thickness.

CFRP with an Impact Damage

Dent size : 2 mm.
C-scan observation : 14 mm.

Simplified Modelling Method

Impact-damaged area :
 > Homogenous
 > Quasi-isotropic
 > Stiffness degradation
 > Frustum of a cone shape

Damage Observation

Delamination is the dominate damage forms.

Theoretical Assumption of Stiffness Degradation

Stiffness Matrix

$$\begin{bmatrix} C_{11} & C_{12} & C_{13} & & & \\ C_{11} & C_{13} & & & & \\ & C_{33} & & & & \\ & & C_{44} & & & \\ & & & C_{44} & & \\ & & & & C_{66} & \end{bmatrix}$$

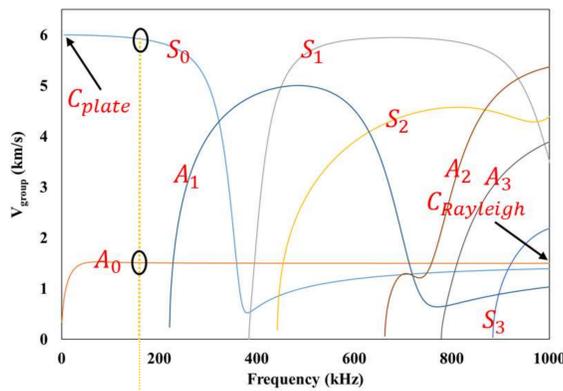
Here, $C_{66} = \frac{C_{11} - C_{12}}{2}$

Quasi-isotropic composite only have **five** independent stiffness coefficients.

$$\begin{cases} C_{11} = \frac{1 - \nu_{23}\nu_{32}}{E_2 E_3 \Delta} \\ C_{12} = \frac{\nu_{21} + \nu_{31}\nu_{23}}{E_2 E_3 \Delta} \\ C_{13} = \frac{\nu_{31} + \nu_{21}\nu_{32}}{E_2 E_3 \Delta} \\ C_{33} = \frac{1 - \nu_{12}\nu_{21}}{E_1 E_2 \Delta} \\ C_{44} = G_{23}, C_{66} = G_{12} \end{cases}$$

Here, $\Delta = \frac{1 - \nu_{12}\nu_{21} - \nu_{23}\nu_{32} - \nu_{13}\nu_{31} - 2\nu_{21}\nu_{32}\nu_{13}}{E_1 E_2 E_3}$

Dispersion of Group Velocity

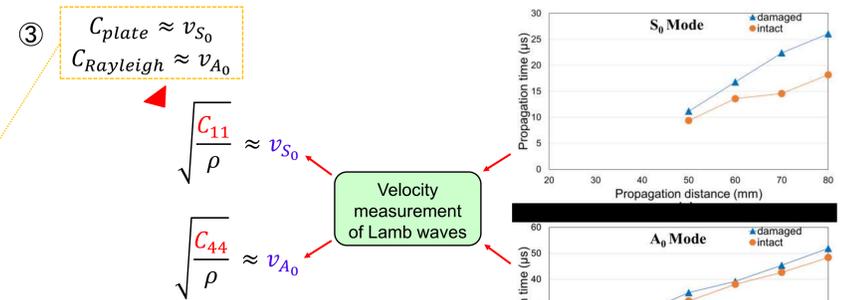


Determination of three coefficients

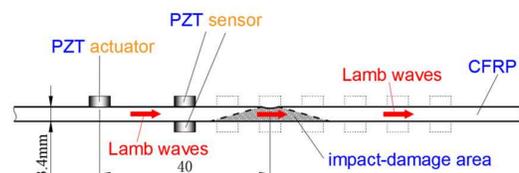
- The stiffness coefficients in thickness direction C_{33} has **little effect** on the velocities of Lamb waves. $\rightarrow C_{33}$ keeps constant.
- ν_{12} is approximately invariant. $\rightarrow C_{12}$ is degraded at the same rate as that of C_{11} .
- Out-of-plane Poisson's ratio is close to 0: $\nu_{31}, \nu_{32} = 0 \rightarrow C_{13} \approx 0$.

Determination of C_{11} and C_{44}

- $C_{plate} = \sqrt{\frac{C_{11}C_{33} - (C_{13})^2}{\rho C_{33}}}$ C_{13} is comparatively small $\rightarrow C_{plate} \approx \sqrt{\frac{C_{11}}{\rho}}$
- $C_{Rayleigh} = \alpha C_{transverse} = \alpha \sqrt{\frac{C_{44}}{\rho}}$ α is close to 1 $\rightarrow C_{Rayleigh} \approx \sqrt{\frac{C_{44}}{\rho}}$

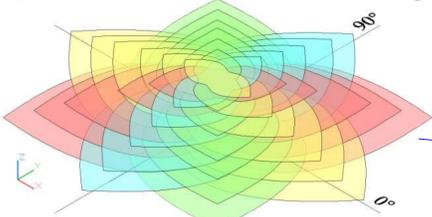


Experiment setup :

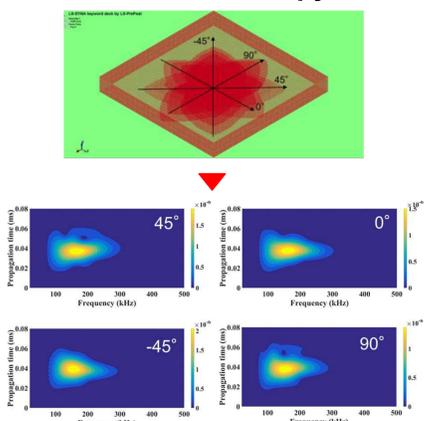


Simulation of Impact Damage

Multiple Delamination in the Damage

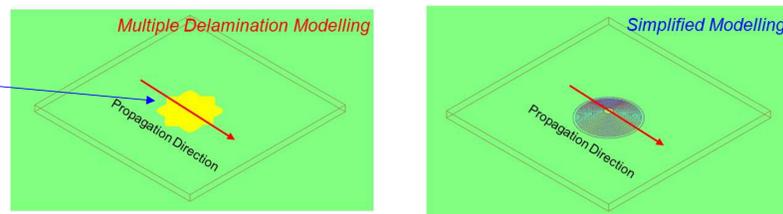


Experimental Confirmation of Quasi-isotropy

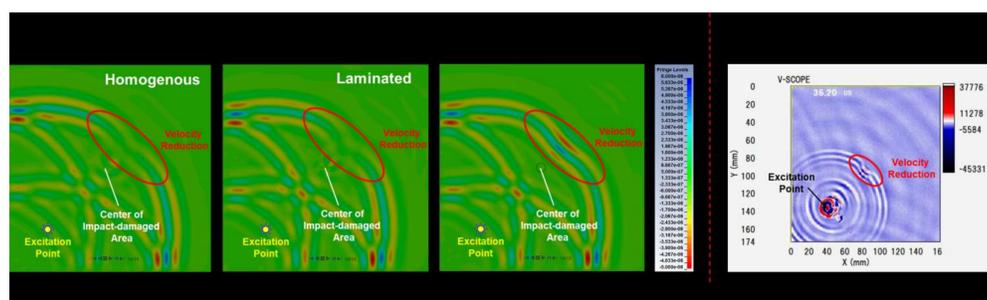


Propagation time and waveform are almost the same in different propagation directions.

Verification of Simplified Modeling Method



Comparison of Wave Propagation Behavior



The agreement between **simulation results** and **experimental observation results** indicates the simplified modelling method is **appropriate** for simulating Lamb wave propagation behavior through impact damages in quasi-isotropic composite structures.

Comparison between Simplified Modeling and Precise Modeling

